


313	46	1
Views	CrossRef citations to date	Altmetric

Prices and Asymptotics for Discrete Variance Swaps

Pages 140-173 | Received 22 Jul 2012, Published online: 01 Aug 2013

 Check for updates

[Full Article](#)
[Figures & data](#)
[References](#)
[Citations](#)
[Metrics](#)

Read this article

We study the fair strike of a discrete variance swap for a general time-homogeneous stochastic volatility model. In the special cases of Heston, Hull-White and Schöbel-Zhu stochastic volatility models, we give simple explicit expressions (improving Broadie and Jain (2008a). The effect of jumps and discrete sampling on volatility and variance swaps. International Journal of Theoretical and Applied Finance, 11(8), 761–797) in the case of the Heston model). We give conditions on parameters under which the fair strike of a discrete variance swap is higher or lower than that of the continuous variance swap. The interest rate and the correlation between the underlying price and its volatility are assumed constant.

variation and applications to options on variance. Working paper. Retrieved from <http://arxiv.org/abs/1103.2310>).

Key Words: Discrete variance swap Heston model Hull-White model Schöbel-Zhu model

View correction statement:
[Erratum](#)

Acknowledgements

Carole Bernard acknowledges support from the Natural Sciences and Engineering Research Council of Canada. Zhenyu Cui acknowledges support from the Bank of Montreal Capital Markets Advanced Research Scholarship. The authors thank Jinyuan Zhang for her help as research assistant, as well as seminar participants Christa Cuchiero, Olympia Hadjiliadis, Antoine Jacquier, Adam Kolkiewicz, Roger Lee, Don McLeish, Johannes Ruf, David Saunders and Michael Suchanecski for helpful suggestions. We are particularly grateful to an anonymous referee for his/her constructive and helpful comments on an earlier draft of this paper.

Notes

- ¹ See, for example, Howison, Rafailidis, and Rasmussenn (2004), Windcliff, Forsyth, and Vetzal (2006), Benth, Groth, and Kufakunesu (2007) and Broadie and Jain (2008b).
 - ² These conditions ensure that we can apply Fubini’s theorem to exchange the order of integration. They are easily verified in specific examples.
 - ³ That
 - ⁴ The
 - ⁵ This
- <http://www>
- well as for all other formulas that appear in this paper.

About Cookies On This Site

We and our partners use cookies to enhance your website experience, learn how our site is used, offer personalised features, measure the effectiveness of our services, and tailor content and ads to your interests while you navigate on the web or interact with us across devices. You can choose to accept all of these cookies or only essential cookies. To learn more or manage your preferences, click “Settings”. For further information about the data we collect from you, please see our [Privacy Policy](#).

Accept All

Essential Only

Settings

6. ⁶ We shall note that here $m(V_t) = V_t$ (where $m(\cdot)$ is defined in (1)) instead of σ , thus the process V_t models the volatility and not the variance. In particular, in the Schöbel-Zhu model, the variance process σ^2 follows $d\sigma^2 = \kappa(\theta - \sigma^2)dt + \eta\sigma dW_t$.
7. ⁷ See Proposition 6.7 for an explicit expansion.
8. ⁸ See Definition 2.6 on p. 112 of Keller-Ressel and Muhle-Karbe (in press).
9. ⁹ This can be easily seen from the fact that for all $t \geq 0$, $V_t \geq 0$, and note that here $\sigma^2 = V_t$.
10. ¹⁰ It reduces to studying the sign of Δ . It is an increasing function of σ , so it is larger than $\Delta|_{\sigma=0}$, which is always positive because its minimum is 0 obtained when $\sigma = 0$.
11. ¹¹ For the two sets of parameters above, we compute the critical interest rate r^* as defined in Remark 2.1. Set 1: $\kappa = 0.1, \theta = 0.05, \eta = 0.1$; Set 2: $\kappa = 0.1, \theta = 0.05, \eta = 0.2$, and we can see that the interest rates are both larger than r^* .
12. ¹² The notation V_t in the Schöbel-Zhu model corresponds to the square root of what is denoted by V_t in the Heston model.
13. ¹³ Note that in terms of our notation, the parameters in Hurd and Kuznetsov (2008) and our parameters have the correspondence $\kappa \leftrightarrow \kappa, \theta \leftrightarrow \theta, \eta \leftrightarrow \eta$.
14. ¹⁴ Note that Δ is a decreasing function in t , thus $\Delta \geq \Delta_n$ is sufficient for $\Delta \geq 0$ for all $i = 0, 1, \dots, n$.

Related research ⓘ

People also read	Recommended articles	Cited by 46
------------------	----------------------	-------------



About Cookies On This Site

We and our partners use cookies to enhance your website experience, learn how our site is used, offer personalised features, measure the effectiveness of our services, and tailor content and ads to your interests while you navigate on the web or interact with us across devices. You can choose to accept all of these cookies or only essential cookies. To learn more or manage your preferences, click “Settings”. For further information about the data we collect from you, please see our [Privacy Policy](#).

- Accept All
- Essential Only
- Settings

Information for

Authors

R&D professionals

Editors

Librarians

Societies

Opportunities

Reprints and e-prints

Advertising solutions

Accelerated publication

Corporate access solutions

Open access

Overview

Open journals

Open Select

Dove Medical Press

F1000Research

Help and information

Help and contact

Newsroom

All journals

Books

Keep up to date

Register to receive personalised research and resources by email



Sign me up



Copyright © 2024 Informa UK Limited [Privacy policy](#) [Cookies](#) [Terms & conditions](#)

[Accessibility](#)



Taylor & Francis Group
an informa business

Registered in England & Wales No. 3099067
5 Howick Place | London | SW1P 1WG

About Cookies On This Site

We and our partners use cookies to enhance your website experience, learn how our site is used, offer personalised features, measure the effectiveness of our services, and tailor content and ads to your interests while you navigate on the web or interact with us across devices. You can choose to accept all of these cookies or only essential cookies. To learn more or manage your preferences, click “Settings”. For further information about the data we collect from you, please see our [Privacy Policy](#).

Accept All

Essential Only

Settings